

# Core 1 Basics Test: Sample Material

Dauntsey's School

No calculators allowed; please answer on file paper.

1: Work out the following:

- a)  $(-1) - (-9) \times 4$       b)  $(-8) \times (-7) - (-3) \times (-5)$       c)  $(-1) + (-5) \times (-5) + 4$   
d)  $(-4) + 6 \times 8$       e)  $(-6) \times 9 + (-4) \times 3$       f)  $8 \times 5 - (-6) \times 1$   
g)  $10 + 2 \times (-4)$       h)  $(-2) + 7 \times 1 + 2$       i)  $3 \times 7 + 4 \times (-10)$   
j)  $9 - (-5) \times 8$       k)  $(-5) + 3 \times (-6) + (-3)$       l)  $(-3) \times (-3) - 6 \times (-2)$   
m)  $5 + (-6) \times (-5)$       n)  $4 \times (-8) + 8 \times 8$       o)  $8 - (-9) \times (-5)$   
p)  $(-2) \times 6 - 3 \times 2$

2: Work out the following, showing your method and giving your answer in its simplest form:

- a)  $2\frac{1}{4} - 1\frac{6}{7}$       b)  $3\frac{1}{5} + 4\frac{1}{3}$       c)  $3\frac{2}{7} - 1\frac{2}{5}$       d)  $4\frac{3}{5} + 2\frac{5}{6}$       e)  $3\frac{1}{6} + 2\frac{2}{7}$       f)  $4\frac{1}{2} - 1\frac{6}{7}$   
g)  $3\frac{1}{8} - 1\frac{3}{5}$       h)  $2\frac{1}{3} + 4\frac{1}{2}$       i)  $2\frac{1}{10} - 1\frac{5}{8}$       j)  $4\frac{1}{4} + 3\frac{5}{6}$       k)  $3\frac{5}{7} - 2\frac{1}{10}$       l)  $4\frac{5}{6} + 1\frac{5}{8}$   
m)  $2\frac{7}{9} + 3\frac{1}{7}$       n)  $4\frac{1}{3} - 1\frac{1}{4}$       o)  $3\frac{1}{8} - 2\frac{5}{9}$       p)  $1\frac{1}{5} + 4\frac{1}{4}$

3: Work out the following, showing your method and giving your answer in its simplest form:

- a)  $1\frac{1}{7} \times 1\frac{1}{4}$       b)  $1\frac{1}{6} \div 4\frac{1}{2}$       c)  $2\frac{1}{2} \times 3\frac{1}{2}$       d)  $1\frac{1}{2} \div 2\frac{1}{4}$       e)  $1\frac{2}{7} \div 1\frac{3}{7}$       f)  $1\frac{1}{5} \times 2\frac{2}{3}$   
g)  $1\frac{3}{4} \times 1\frac{1}{9}$       h)  $1\frac{3}{5} \div 1\frac{1}{3}$       i)  $3\frac{1}{3} \times 1\frac{2}{5}$       j)  $1\frac{2}{3} \div 1\frac{4}{5}$       k)  $1\frac{1}{8} \div 2\frac{1}{3}$       l)  $1\frac{1}{6} \times 2\frac{1}{4}$   
m)  $1\frac{1}{7} \div 3\frac{1}{2}$       n)  $1\frac{1}{4} \times 1\frac{1}{3}$       o)  $2\frac{1}{2} \div 4\frac{1}{2}$       p)  $1\frac{1}{9} \times 2\frac{2}{3}$

4: Simplify the following:

- a)  $2w^4y^2 \times 5w^7y^9$       b)  $(2z^8r^2)^2$       c)  $\frac{6g^{10}s^{10}}{3g^9s^6}$       d)  $3bv \times 4b^8v^6$       e)  $\frac{20k^6n^{18}}{5k^3n^{10}}$   
f)  $(4u^2e^9)^2$       g)  $(3q^6h^{10})^3$       h)  $5x^2a^{10} \times 6x^7a^5$       i)  $\frac{15t^4j^{14}}{5t^3j^4}$       j)  $\frac{12m^{15}c^5}{4m^8c^3}$   
k)  $(5d^7p^3)^3$       l)  $4f^{10}l^6 \times 5f^{10}l^3$       m)  $\frac{6r^{17}e^{19}}{3r^7e^{10}}$       n)  $(4q^{10}n)^2$       o)  $2g^4v \times 5g^5v^8$   
p)  $(2w^6h^7)^3$       q)  $\frac{30t^{16}u^{15}}{6t^7u^8}$       r)  $3k^5l^9 \times 5k^2l^3$       s)  $\frac{12f^7z^{12}}{4f^2z^2}$       t)  $4p^7a^4 \times 5p^{10}a^8$   
u)  $(3x^8y)^2$       v)  $\frac{6l^5c^8}{3f^6c^4}$       w)  $(5bs^3)^3$       x)  $2m^9d^3 \times 5m^9d^2$

5: Work out the following:

- a)  $5^0$       b)  $8^{-1}$       c)  $10^{-1}$       d)  $10^0$       e)  $10^{-2}$       f)  $1^0$   
g)  $1^{-3}$       h)  $3^0$       i)  $4^{-2}$       j)  $6^0$       k)  $8^0$       l)  $5^{-1}$   
m)  $2^{-3}$       n)  $7^0$       o)  $2^{-2}$       p)  $4^0$

6: Work out the following:

- a)  $2500^{-1/2}$       b)  $9^{1/2}$       c)  $27^{-1/3}$       d)  $4^{1/2}$       e)  $8^{-1/3}$       f)  $36^{1/2}$   
g)  $1^{1/3}$       h)  $1000^{-1/3}$       i)  $25^{-1/2}$       j)  $16^{1/2}$       k)  $125^{-1/3}$       l)  $81^{1/2}$   
m)  $400^{1/2}$       n)  $64^{-1/2}$       o)  $9^{-1/2}$       p)  $4^{1/2}$

7: Simplify the following surds:

- a)  $\sqrt{250} - \sqrt{90}$       b)  $\sqrt{160} + \sqrt{40}$       c)  $\sqrt{90} + \sqrt{250}$       d)  $\sqrt{80} - \sqrt{20}$       e)  $\sqrt{48} + \sqrt{27}$       f)  $\sqrt{27} - \sqrt{3}$

g) $\sqrt{45} - \sqrt{20}$	h) $\sqrt{12} + \sqrt{3}$	i) $\sqrt{125} + \sqrt{80}$	j) $\sqrt{175} - \sqrt{63}$	k) $\sqrt{40} - \sqrt{10}$	l) $\sqrt{63} + \sqrt{112}$
m) $\sqrt{18} - \sqrt{8}$	n) $\sqrt{96} + \sqrt{6}$	o) $\sqrt{54} - \sqrt{6}$	p) $\sqrt{32} + \sqrt{18}$		

8: Simplify the following surds:

a) $\frac{10}{\sqrt{3}}$	b) $\frac{1}{\sqrt{10}}$	c) $\frac{3}{\sqrt{2}}$	d) $\frac{5}{\sqrt{7}}$
e) $\frac{4}{\sqrt{3}}$	f) $\frac{3}{\sqrt{10}}$	g) $\frac{4}{\sqrt{5}}$	h) $\frac{7}{\sqrt{10}}$

9: Simplify the following surds:

a) $(6 + \sqrt{5})^2$	b) $(1 + \sqrt{3})^2$	c) $(3 - \sqrt{10})^2$	d) $(2 - \sqrt{7})^2$
e) $(4 + \sqrt{6})^2$	f) $(5 - \sqrt{2})^2$	g) $(3 + \sqrt{3})^2$	h) $(6 - \sqrt{7})^2$

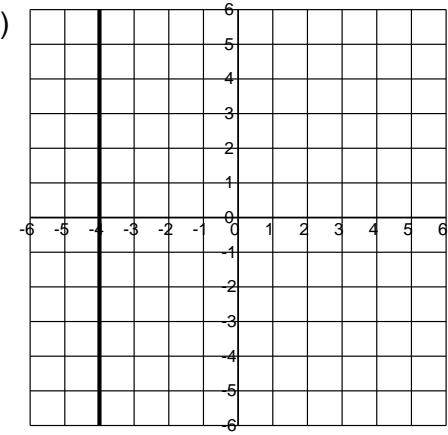
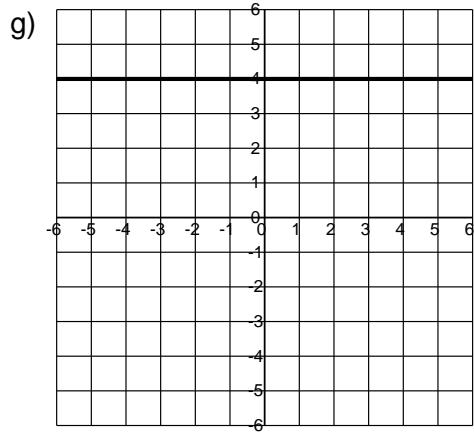
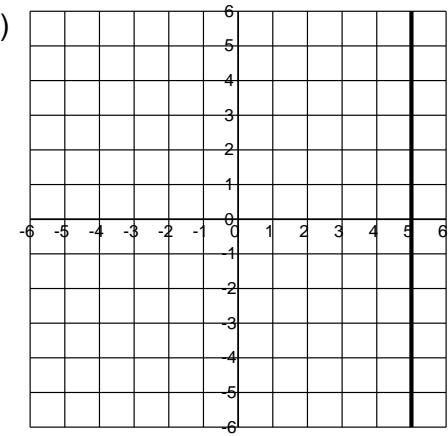
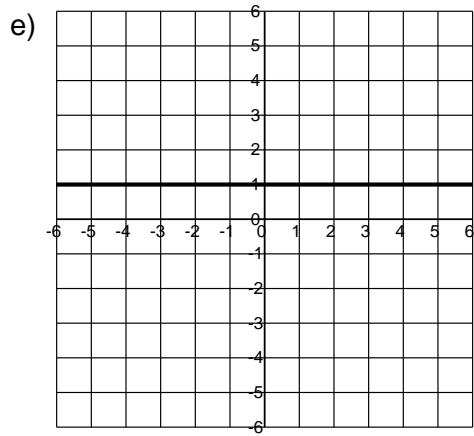
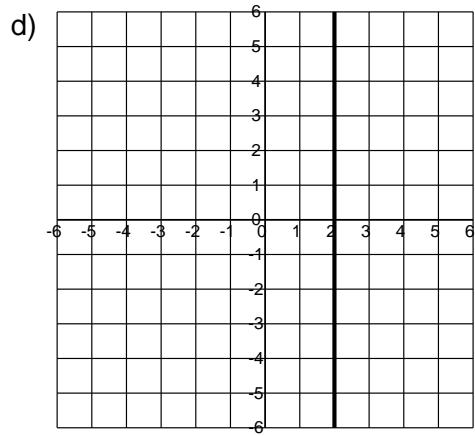
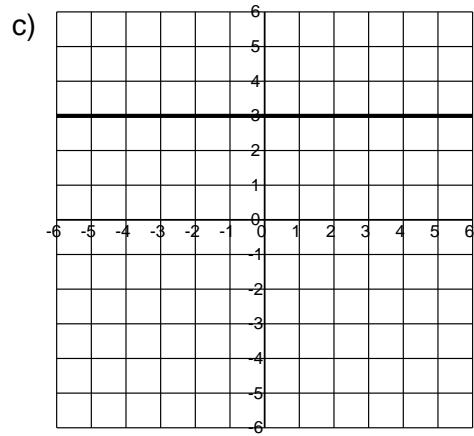
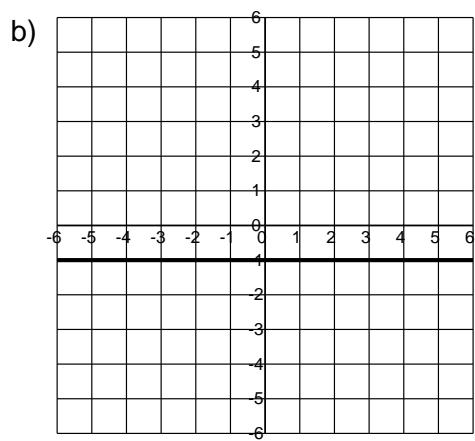
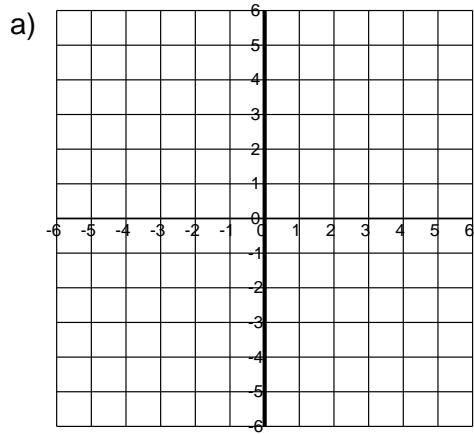
10: Solve the following:

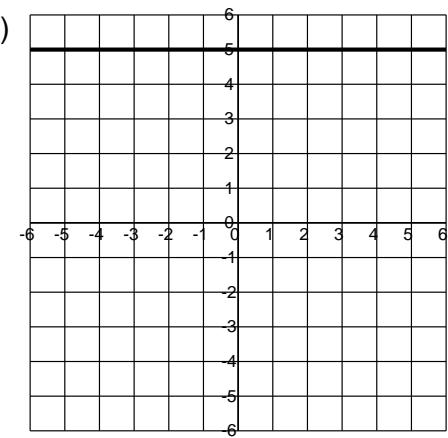
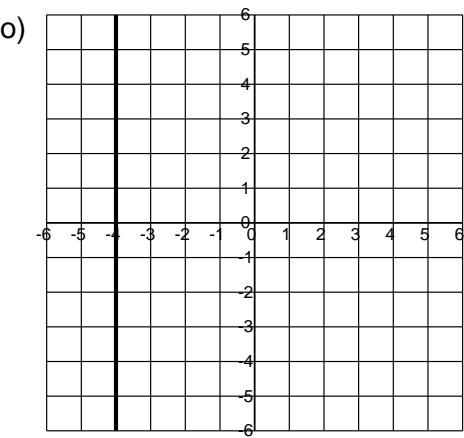
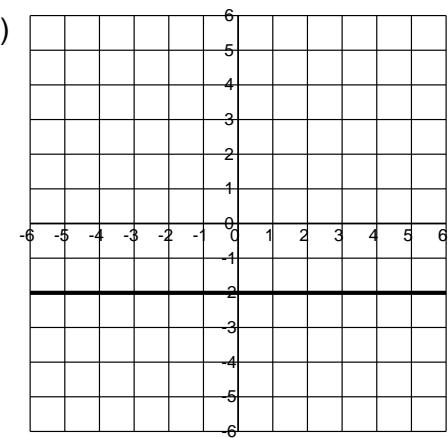
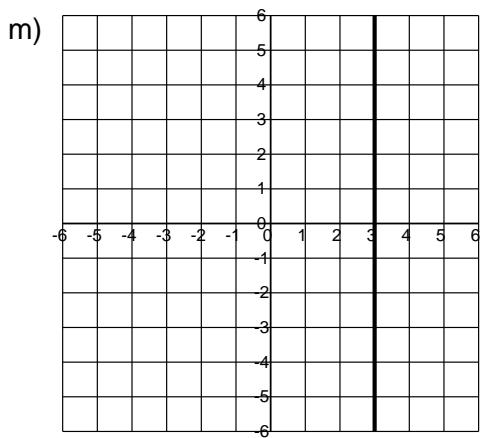
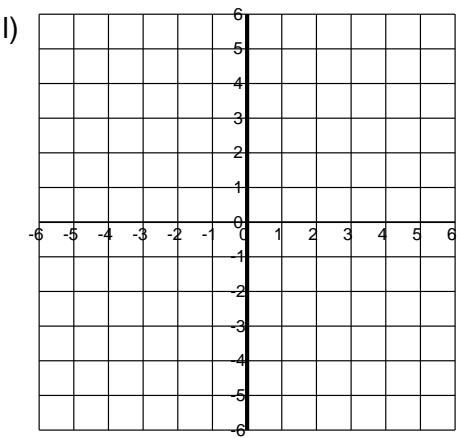
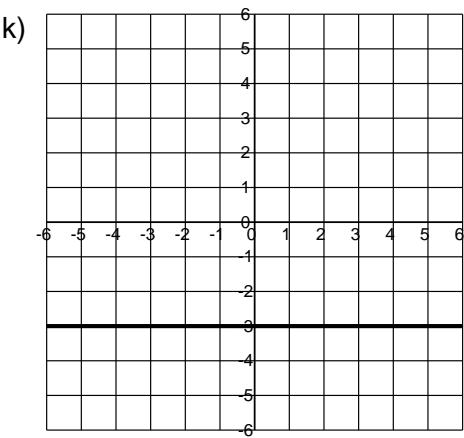
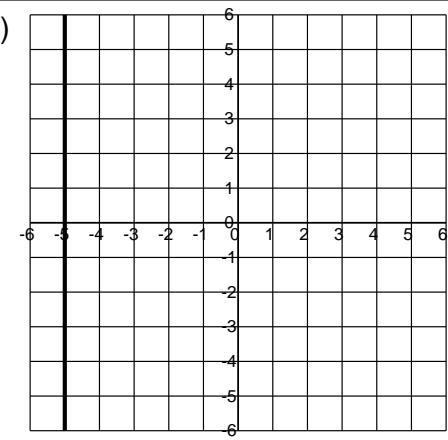
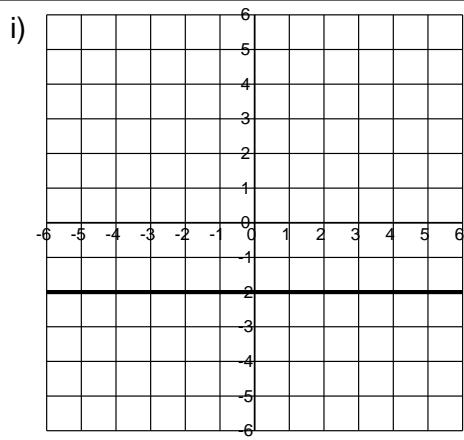
a) $-10(x - 8) > 170$	b) $-x - 10 \geq -19$	c) $-9x + 9 < 9$	d) $-6x \leq -30$
e) $-3x > 18$	f) $-x - 9 \geq -15$	g) $-8x + 10 < -70$	h) $-4(x + 2) \leq 0$
i) $-x - 4 < -1$	j) $-6x \geq 24$	k) $-10x + 5 > -35$	l) $-5(x - 7) \leq 30$
m) $-3(x - 6) < 21$	n) $-8x \geq -56$	o) $-x - 5 > 2$	p) $-2x + 3 \leq 19$

11: Solve the following inequalities:

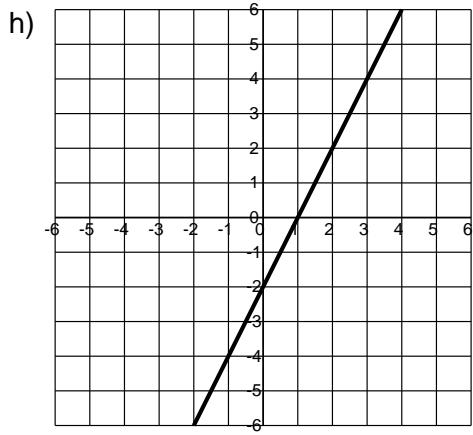
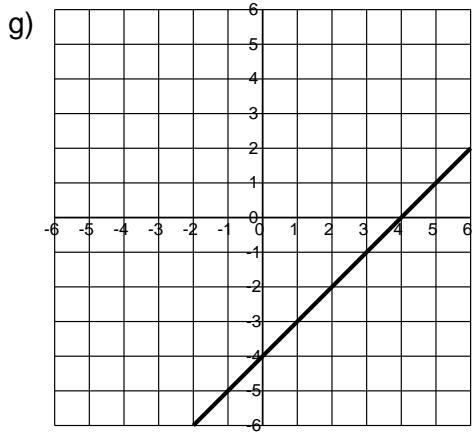
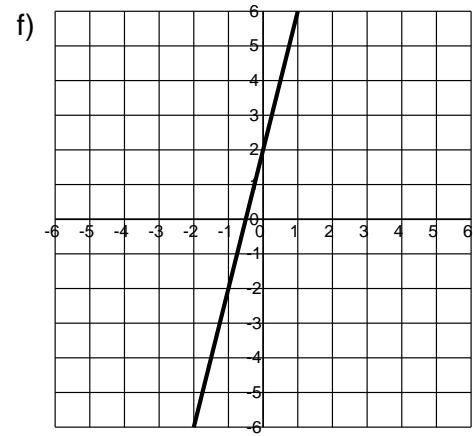
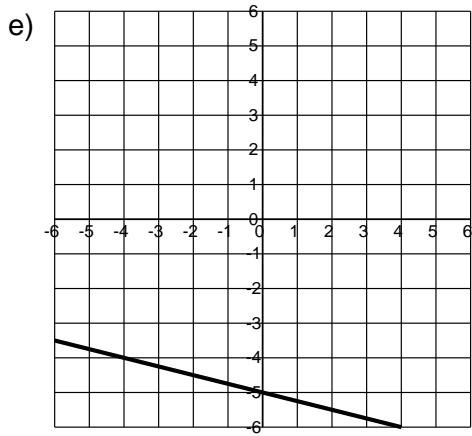
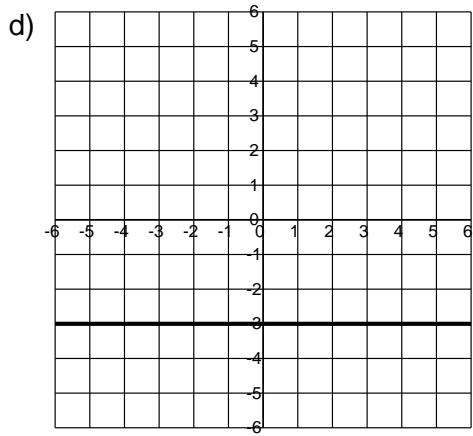
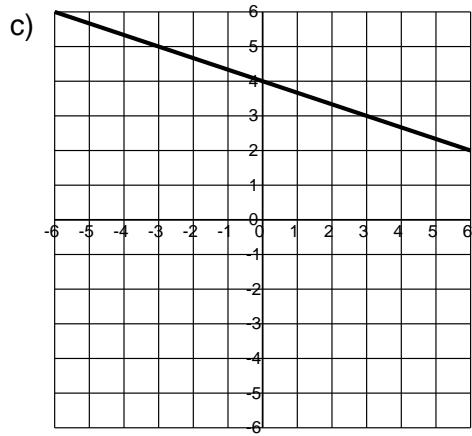
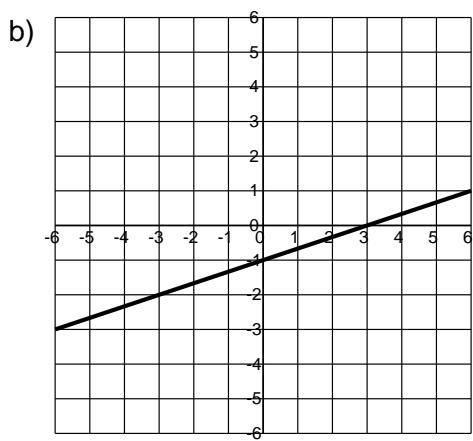
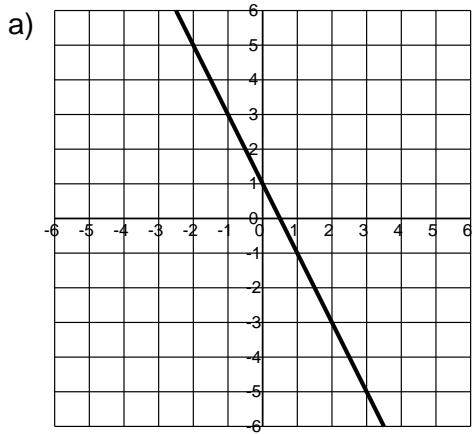
a) $2x^2 + 9 < 17$	b) $4x^2 - 3 > 321$	c) $3x^2 + 14 \leq 41$	d) $4x^2 + 19 \geq 163$	e) $3x^2 + 11 > 158$
f) $2x^2 - 2 < 0$	g) $2x^2 + 14 \leq 214$	h) $4x^2 + 6 \geq 106$	i) $3x^2 - 3 > 45$	j) $2x^2 - 19 < 109$
k) $3x^2 - 19 \leq -7$	l) $4x^2 - 1 \geq 323$	m) $2x^2 + 11 \leq 109$	n) $4x^2 + 8 < 152$	o) $3x^2 + 15 > 63$
p) $4x^2 + 5 \geq 261$				

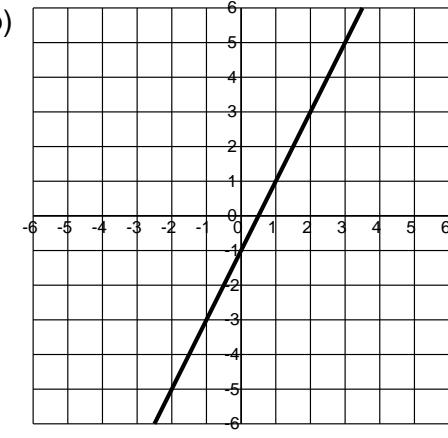
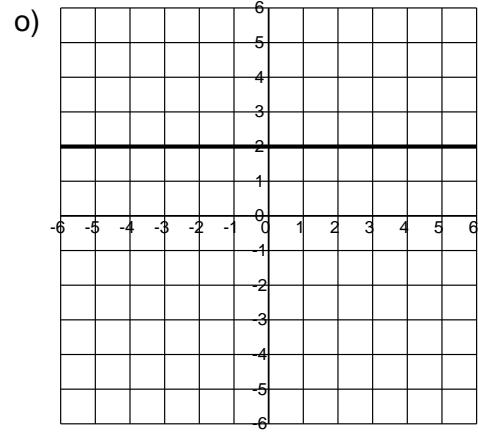
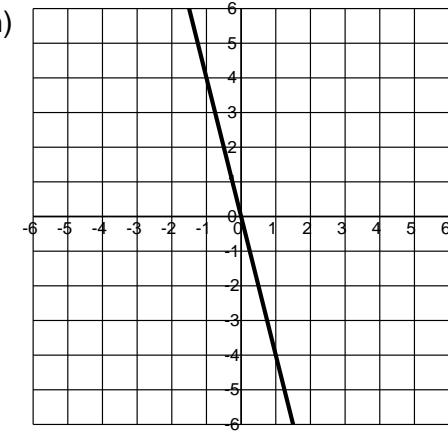
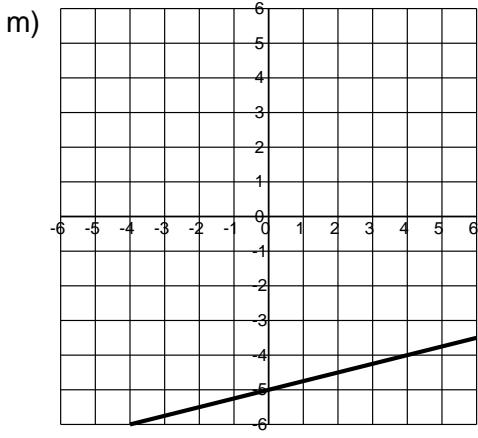
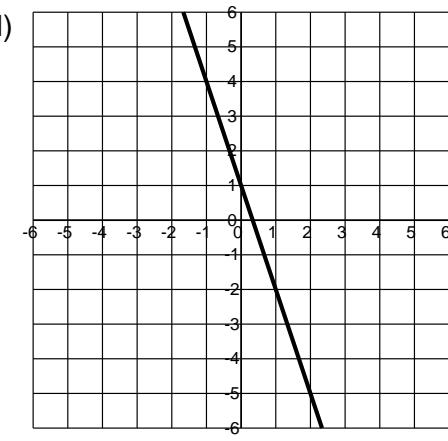
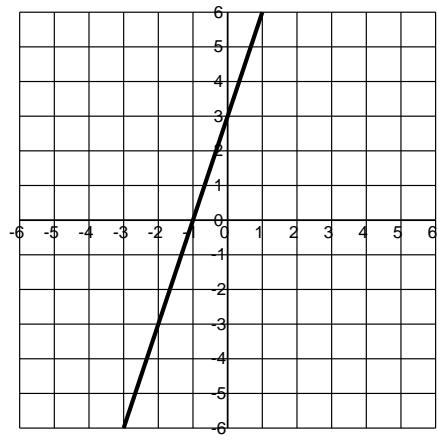
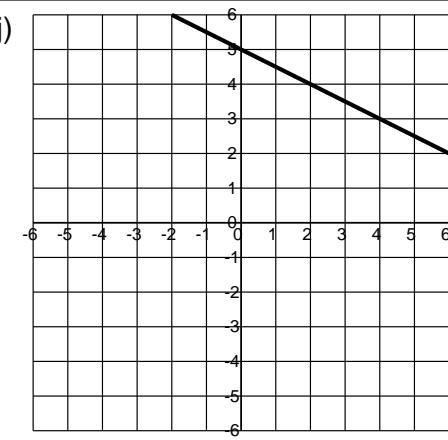
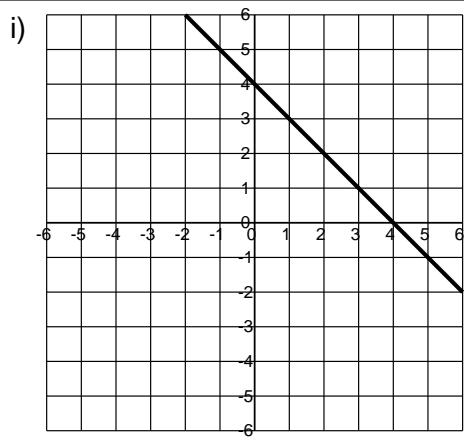
12: Give equations for the following graphs:





13: Give equations for the following graphs:





14: Work out the following:

- a) A line segment is drawn between (0, 10) and (3, 7). Find its gradient, mid-point and length.
- b) A line segment is drawn between (3, 1) and (4, 2). Find its gradient, mid-point and length.
- c) A line segment is drawn between (5, 9) and (7, 7). Find its gradient, mid-point and length.
- d) A line segment is drawn between (3, 5) and (8, 7). Find its gradient, mid-point and length.
- e) A line segment is drawn between (4, 6) and (8, 2). Find its gradient, mid-point and length.
- f) A line segment is drawn between (1, 0) and (4, 5). Find its gradient, mid-point and length.
- g) A line segment is drawn between (6, 3) and (8, 7). Find its gradient, mid-point and length.
- h) A line segment is drawn between (8, 5) and (9, 5). Find its gradient, mid-point and length.
- i) A line segment is drawn between (2, 9) and (7, 8). Find its gradient, mid-point and length.
- j) A line segment is drawn between (2, 2) and (6, 5). Find its gradient, mid-point and length.
- k) A line segment is drawn between (1, 10) and (2, 5). Find its gradient, mid-point and length.
- l) A line segment is drawn between (1, 5) and (4, 2). Find its gradient, mid-point and length.
- m) A line segment is drawn between (3, 4) and (5, 6). Find its gradient, mid-point and length.
- n) A line segment is drawn between (3, 4) and (8, 0). Find its gradient, mid-point and length.
- o) A line segment is drawn between (2, 7) and (3, 6). Find its gradient, mid-point and length.
- p) A line segment is drawn between (6, 4) and (10, 5). Find its gradient, mid-point and length.

15: Multiply out and simplify the following:

- a)  $(-7n + 9)(5n - 4)$
- b)  $(-2f + 7)(7f - 10)$
- c)  $(-6g - 8)(2g - 3)$
- d)  $(-9u + 1)(-7u - 7)$
- e)  $(2k - 7)(4k - 6)$
- f)  $(2w + 4)(-9w + 4)$
- g)  $(6h + 8)(-2h - 8)$
- h)  $(-8r + 9)(-6r - 1)$

16: Solve by factorising:

- a)  $e^2 - 14e + 48 = 0$
- b)  $p^2 - 9 = 0$
- c)  $m^2 - 4m + 4 = 0$
- d)  $c^2 + 10c + 16 = 0$
- e)  $y^2 + 4y = 0$
- f)  $v^2 - 36 = 0$
- g)  $z^2 + 3z - 10 = 0$
- h)  $\ell^2 - l = 0$
- i)  $h^2 - 6h + 9 = 0$
- j)  $p^2 - 100 = 0$
- k)  $n^2 + 17n + 70 = 0$
- l)  $f^2 - 13f + 42 = 0$
- m)  $b^2 - 18b + 81 = 0$
- n)  $g^2 - 7g + 6 = 0$
- o)  $x^2 + 5x - 36 = 0$
- p)  $a^2 + 6a = 0$

17: Factorise the following:

- a)  $12t^2 - 13t + 3$
- b)  $36s^2 + 13s + 1$
- c)  $4d^2 + 11d - 3$
- d)  $40c^2 - 11c - 2$
- e)  $24v^2 - 13v - 2$
- f)  $50r^2 - 15r + 1$
- g)  $5u^2 - 43u - 18$
- h)  $12q^2 - 32q + 5$

18: Solve using the quadratic formula, giving your answer in simplified surd form:

- a)  $-2m^2 + 9m + 4 = 0$
- b)  $-5b^2 - 7b + 2 = 0$
- c)  $3e^2 - 5e - 1 = 0$
- d)  $-5n^2 + 5n + 5 = 0$
- e)  $5t^2 - 10t - 3 = 0$
- f)  $-4f^2 + 7f + 4 = 0$
- g)  $3w^2 - 6w - 4 = 0$
- h)  $3a^2 + 10a + 4 = 0$

19: Solve the following simultaneous equations:

- a)  $v = x^2 - 4x - 17$   
 $v = -3x - 5$
- b)  $k = \ell^2 - 3\ell + 8$   
 $k = 2\ell + 2$
- c)  $c = j^2 + j + 11$   
 $c = -5j + 3$
- d)  $z = q^2 + 9q + 1$   
 $z = 4q - 5$
- e)  $h = n^2 + 4n - 4$   
 $h = 5n - 2$
- f)  $b = y^2 - 2y - 10$   
 $b = -y - 4$
- g)  $s = w^2 - 3w + 17$   
 $s = 4w + 5$
- h)  $t = \ell^2 - 8\ell - 8$   
 $t = -5\ell + 2$

20: Simplify the following as far as possible:

- a)  $\frac{12f^2 + 12f}{8f^2 + 16f}$
- b)  $\frac{2v^2 - 3v}{3v^2 - v}$
- c)  $\frac{90a^2 + 30a}{24a}$
- d)  $\frac{4d^2 + 16d}{6d}$
- e)  $\frac{z^2 + 3z}{2z^2 + 3z}$
- f)  $\frac{27p^2 - 18p}{24p^2 + 12p}$

g)  $\frac{8u^2 - 8u}{20u}$

h)  $\frac{q^2 - 3q}{2q^2 - q}$

i)  $\frac{20m^2 - 40m}{15m^2 - 60m}$

j)  $\frac{3c^2 + 2c}{3c^2 - 2c}$

k)  $\frac{2k^2 + 4k}{18k^2 + 6k}$

l)  $\frac{9x^2 - 3x}{6x}$

m)  $\frac{j^2 - j}{j^2 + 3j}$

n)  $\frac{30r^2 + 45r}{25r}$

o)  $\frac{3e^2 + 3e}{15e^2 - 60e}$

p)  $\frac{2g^2 - 3g}{2g^2 + g}$

21: Simplify the following as far as possible:

a)  $\frac{s-3}{2} - \frac{2s-1}{6}$

b)  $\frac{3n+2}{3} + \frac{n+4}{2}$

c)  $\frac{z-2}{4} + \frac{z-1}{2}$

d)  $\frac{7(3y-2)}{8} - \frac{3y-1}{2}$

e)  $\frac{2d+3}{5} + \frac{2(3d+1)}{3}$

f)  $\frac{7(t+2)}{10} - \frac{t-3}{5}$

g)  $\frac{2w-3}{9} + \frac{5(w-2)}{6}$

h)  $\frac{2(v+1)}{3} - \frac{2(2v-1)}{9}$

i)  $\frac{b-4}{6} + \frac{b+4}{4}$

j)  $\frac{3u+2}{8} + \frac{3(u+3)}{4}$

k)  $\frac{3(2m+1)}{5} - \frac{m-2}{2}$

l)  $\frac{9(c-1)}{10} - \frac{3c-1}{2}$

m)  $\frac{r+2}{6} + \frac{2(3r+1)}{3}$

n)  $\frac{a+1}{4} - \frac{3a-2}{10}$

o)  $\frac{h-4}{4} + \frac{2(2h+1)}{3}$

p)  $\frac{2(2k+3)}{3} - \frac{2(k-3)}{9}$

22: Simplify the following as far as possible:

a)  $\frac{4}{7f} \times \frac{3}{5f}$

b)  $\frac{9g}{4} \div \frac{5}{2g}$

c)  $\frac{3q}{2} \div \frac{3q}{4}$

d)  $\frac{7}{2j} \times \frac{9j}{2}$

e)  $\frac{7l}{6} \div \frac{3l}{10}$

f)  $\frac{9p}{10} \times \frac{9}{7p}$

g)  $\frac{3}{7e} \times \frac{7}{5e}$

h)  $\frac{4}{5x} \div \frac{5x}{9}$

i)  $\frac{5}{8n} \div \frac{8}{9n}$

j)  $\frac{4s}{7} \times \frac{6}{5s}$

k)  $\frac{8d}{3} \div \frac{3d}{5}$

l)  $\frac{8}{7u} \times \frac{10u}{7}$

m)  $\frac{2}{7b} \times \frac{9}{4b}$

n)  $\frac{6v}{7} \div \frac{5v}{2}$

o)  $\frac{9w}{10} \div \frac{5}{9w}$

p)  $\frac{9}{8m} \times \frac{2m}{3}$

# Answers: Core 1 Basics Test: Sample Material

Dauntsey's School

- |          |       |        |        |        |       |
|----------|-------|--------|--------|--------|-------|
| 1: a) 35 | b) 41 | c) 28  | d) 44  | e) -66 | f) 46 |
| g) 2     | h) 7  | i) -19 | j) 49  | k) -26 | l) 21 |
| m) 35    | n) 32 | o) -37 | p) -18 |        |       |

- |  |   |   |   |  |
|--|---|---|---|--|
| 2: a) $2\frac{7}{28} - 1\frac{24}{28} = \frac{11}{28}$ | b) $3\frac{3}{15} + 4\frac{5}{15} = 7\frac{8}{15}$    | c) $3\frac{10}{35} - 1\frac{14}{35} = 1\frac{31}{35}$ | d) $4\frac{18}{30} + 2\frac{25}{30} = 7\frac{13}{30}$ | e) $3\frac{7}{42} + 2\frac{12}{42} = 5\frac{19}{42}$ |
| f) $4\frac{7}{14} - 1\frac{12}{14} = 2\frac{9}{14}$    | g) $3\frac{5}{40} - 1\frac{24}{40} = 1\frac{21}{40}$  | h) $2\frac{2}{6} + 4\frac{3}{6} = 6\frac{5}{6}$       | i) $2\frac{4}{40} - 1\frac{25}{40} = \frac{19}{40}$   | j) $4\frac{3}{12} + 3\frac{10}{12} = 8\frac{1}{12}$  |
| k) $3\frac{50}{70} - 2\frac{7}{70} = 1\frac{43}{70}$   | l) $4\frac{20}{24} + 1\frac{15}{24} = 6\frac{11}{24}$ | m) $2\frac{49}{63} + 3\frac{9}{63} = 5\frac{58}{63}$  | n) $4\frac{4}{12} - 1\frac{3}{12} = 3\frac{1}{12}$    | o) $3\frac{9}{72} - 2\frac{40}{72} = \frac{41}{72}$  |
| p) $1\frac{4}{20} + 4\frac{5}{20} = 5\frac{9}{20}$     |   |   |   |  |

- |   |  |   |
|---|--|---|
| 3: a) $\frac{8}{7} \times \frac{5}{4} = \frac{2}{7} \times \frac{5}{1} = \frac{10}{7} = 1\frac{3}{7}$             | b) $\frac{7}{6} \div \frac{9}{2} = \frac{7}{6} \times \frac{2}{9} = \frac{7}{3} \times \frac{1}{9} = \frac{7}{27}$               | c) $\frac{5}{2} \times \frac{7}{2} = \frac{35}{4} = 8\frac{3}{4}$   |
| d) $\frac{3}{2} \div \frac{9}{4} = \frac{3}{2} \times \frac{4}{9} = \frac{1}{1} \times \frac{2}{3} = \frac{2}{3}$ | e) $\frac{9}{7} \div \frac{10}{7} = \frac{9}{7} \times \frac{7}{10} = \frac{9}{1} \times \frac{1}{10} = \frac{9}{10}$            | f) $\frac{6}{5} \times \frac{8}{3} = \frac{2}{5} \times \frac{8}{1} = \frac{16}{5} = 3\frac{1}{5}$                |
| g) $\frac{7}{4} \times \frac{10}{9} = \frac{7}{2} \times \frac{5}{9} = \frac{35}{18} = 1\frac{17}{18}$            | h) $\frac{8}{5} \div \frac{4}{3} = \frac{8}{5} \times \frac{3}{4} = \frac{2}{5} \times \frac{3}{1} = \frac{6}{5} = 1\frac{1}{5}$ | i) $\frac{10}{3} \times \frac{7}{5} = \frac{2}{3} \times \frac{7}{1} = \frac{14}{3} = 4\frac{2}{3}$               |
| j) $\frac{5}{3} \div \frac{9}{5} = \frac{5}{3} \times \frac{5}{9} = \frac{25}{27}$                                | k) $\frac{9}{8} \div \frac{7}{3} = \frac{9}{8} \times \frac{3}{7} = \frac{27}{56}$   | l) $\frac{7}{6} \times \frac{9}{4} = \frac{7}{2} \times \frac{3}{4} = \frac{21}{8} = 2\frac{5}{8}$                |
| m) $\frac{8}{7} \div \frac{7}{2} = \frac{8}{7} \times \frac{2}{7} = \frac{16}{49}$                                | n) $\frac{5}{4} \times \frac{4}{3} = \frac{5}{1} \times \frac{1}{3} = \frac{5}{3} = 1\frac{2}{3}$                                | o) $\frac{5}{2} \div \frac{9}{2} = \frac{5}{2} \times \frac{2}{9} = \frac{5}{1} \times \frac{1}{9} = \frac{5}{9}$ |
| p) $\frac{10}{9} \times \frac{8}{3} = \frac{80}{27} = 2\frac{26}{27}$   |  |   |

- |                        |                     |                 |                    |                   |                  |
|------------------------|---------------------|-----------------|--------------------|-------------------|------------------|
| 4: a) $10w^{11}y^{11}$ | b) $4z^{16}r^4$     | c) $2gs^4$      | d) $12b^9v^7$      | e) $4K^3n^8$      | f) $16u^4e^{18}$ |
| g) $27q^{18}h^{30}$    | h) $30x^9a^{15}$    | i) $3tj^{10}$   | j) $3m^7c^2$       | k) $125d^{21}p^9$ | l) $20f^{20}p^0$ |
| m) $2r^{10}e^9$        | n) $16q^{20}n^2$    | o) $10g^9v^9$   | p) $8w^{18}h^{21}$ | q) $5t^6u^7$      | r) $15k^7j^{12}$ |
| s) $3f^5z^{10}$        | t) $20p^{17}a^{12}$ | u) $9x^{16}y^2$ | v) $2t^8c^4$       | w) $125b^3s^9$    | x) $10m^{18}d^6$ |

- |                  |                  |                   |      |                    |                  |
|------------------|------------------|-------------------|------|--------------------|------------------|
| 5: a) 1          | b) $\frac{1}{8}$ | c) $\frac{1}{10}$ | d) 1 | e) $\frac{1}{100}$ | f) 1             |
| g) 1             | h) 1             | i) $\frac{1}{16}$ | j) 1 | k) 1               | l) $\frac{1}{5}$ |
| m) $\frac{1}{8}$ | n) 1             | o) $\frac{1}{4}$  | p) 1 |                    |                  |

- |                      |                   |                  |      |                  |      |
|----------------------|-------------------|------------------|------|------------------|------|
| 6: a) $\frac{1}{50}$ | b) 3              | c) $\frac{1}{3}$ | d) 2 | e) $\frac{1}{2}$ | f) 6 |
| g) 1                 | h) $\frac{1}{10}$ | i) $\frac{1}{5}$ | j) 4 | k) $\frac{1}{5}$ | l) 9 |
| m) 20                | n) $\frac{1}{8}$  | o) $\frac{1}{3}$ | p) 2 |                  |      |

- |                    |                 |                 |                |                |                |
|--------------------|-----------------|-----------------|----------------|----------------|----------------|
| 7: a) $2\sqrt{10}$ | b) $6\sqrt{10}$ | c) $8\sqrt{10}$ | d) $2\sqrt{5}$ | e) $7\sqrt{3}$ | f) $2\sqrt{3}$ |
| g) $\sqrt{5}$      | h) $3\sqrt{3}$  | i) $9\sqrt{5}$  | j) $2\sqrt{7}$ | k) $\sqrt{10}$ | l) $7\sqrt{7}$ |
| m) $\sqrt{2}$      | n) $5\sqrt{6}$  | o) $2\sqrt{6}$  | p) $7\sqrt{2}$ |                |                |

- |                              |                            |                          |                            |
|------------------------------|----------------------------|--------------------------|----------------------------|
| 8: a) $\frac{10\sqrt{3}}{3}$ | b) $\frac{\sqrt{10}}{10}$  | c) $\frac{3\sqrt{2}}{2}$ | d) $\frac{5\sqrt{7}}{7}$   |
| e) $\frac{4\sqrt{3}}{3}$     | f) $\frac{3\sqrt{10}}{10}$ | g) $\frac{4\sqrt{5}}{5}$ | h) $\frac{7\sqrt{10}}{10}$ |

- |                         |                      |                      |                      |
|-------------------------|----------------------|----------------------|----------------------|
| 9: a) $41 + 12\sqrt{5}$ | b) $4 + 2\sqrt{3}$   | c) $19 - 6\sqrt{10}$ | d) $11 - 4\sqrt{7}$  |
| e) $22 + 8\sqrt{6}$     | f) $27 - 10\sqrt{2}$ | g) $12 + 6\sqrt{3}$  | h) $43 - 12\sqrt{7}$ |

- |                 |                |             |                |             |               |
|-----------------|----------------|-------------|----------------|-------------|---------------|
| 10: a) $x < -9$ | b) $x \leq 9$  | c) $x > 0$  | d) $x \geq 5$  | e) $x < -6$ | f) $x \leq 6$ |
| g) $x > 10$     | h) $x \geq -2$ | i) $x > -3$ | j) $x \leq -4$ | k) $x < 4$  | l) $x \geq 1$ |
| m) $x > -1$     | n) $x \leq 7$  | o) $x < -7$ | p) $x \geq -8$ |             |               |

11: a) $-2 < x < 2$	b) $x < -9$ or $x > 9$	c) $-3 \leq x \leq 3$	d) $x \leq -6$ or $x \geq 6$
e) $x < -7$ or $x > 7$	f) $-1 < x < 1$	g) $-10 \leq x \leq 10$	h) $x \leq -5$ or $x \geq 5$
i) $x < -4$ or $x > 4$	j) $-8 < x < 8$	k) $-2 \leq x \leq 2$	l) $x \leq -9$ or $x \geq 9$
m) $-7 \leq x \leq 7$	n) $-6 < x < 6$	o) $x < -4$ or $x > 4$	p) $x \leq -8$ or $x \geq 8$
12: a) $x = 0$	b) $y = -1$	c) $y = 3$	d) $x = 2$
g) $y = 4$	h) $x = -4$	i) $y = -2$	j) $x = -5$
m) $x = 3$	n) $y = -2$	o) $x = -4$	p) $y = 5$
13: a) $y = -2x + 1$	b) $y = \frac{1}{3}x - 1$	c) $y = -\frac{1}{3}x + 4$	d) $y = -3$
g) $y = x - 4$	h) $y = 2x - 2$	i) $y = -x + 4$	j) $y = -\frac{1}{2}x + 5$
m) $y = \frac{1}{4}x - 5$	n) $y = -4x$	o) $y = 2$	p) $y = 2x - 1$
14: a) Gradient = $-1$ Mid-point = $(1.5, 8.5)$ Length = $\sqrt{18}$	b) Gradient = $1$ Mid-point = $(3.5, 1.5)$ Length = $\sqrt{2}$	c) Gradient = $-1$ Mid-point = $(6, 8)$ Length = $\sqrt{8}$	d) Gradient = $\frac{2}{5}$ Mid-point = $(5.5, 6)$ Length = $\sqrt{29}$
e) Gradient = $-1$ Mid-point = $(6, 4)$ Length = $\sqrt{32}$	f) Gradient = $\frac{5}{3}$ Mid-point = $(2.5, 2.5)$ Length = $\sqrt{34}$	g) Gradient = $2$ Mid-point = $(7, 5)$ Length = $\sqrt{20}$	h) Gradient = $0$ Mid-point = $(8.5, 5)$ Length = $\sqrt{1} = 1$
i) Gradient = $-\frac{1}{5}$ Mid-point = $(4.5, 8.5)$ Length = $\sqrt{26}$	j) Gradient = $\frac{3}{4}$ Mid-point = $(4, 3.5)$ Length = $\sqrt{25} = 5$	k) Gradient = $-5$ Mid-point = $(1.5, 7.5)$ Length = $\sqrt{26}$	l) Gradient = $-1$ Mid-point = $(2.5, 3.5)$ Length = $\sqrt{18}$
m) Gradient = $1$ Mid-point = $(4, 5)$ Length = $\sqrt{8}$	n) Gradient = $-\frac{4}{5}$ Mid-point = $(5.5, 2)$ Length = $\sqrt{41}$	o) Gradient = $-1$ Mid-point = $(2.5, 6.5)$ Length = $\sqrt{2}$	p) Gradient = $\frac{1}{4}$ Mid-point = $(8, 4.5)$ Length = $\sqrt{17}$
15: a) $-35n^2 + 73n - 36$	b) $-14f^2 + 69f - 70$	c) $-12g^2 + 2g + 24$	d) $63u^2 + 56u - 7$
e) $8k^2 - 40k + 42$	f) $-18w^2 - 28w + 16$	g) $-12h^2 - 64h - 64$	h) $48r^2 - 46r - 9$
16: a) $e = 6, e = 8$	b) $p = -3, p = 3$	c) $m = 2$	d) $c = -2, c = -8$
f) $v = 6, v = -6$	g) $z = 2, z = -5$	h) $l = 0, l = 1$	i) $h = 3$
k) $n = -10, n = -7$	l) $f = 7, f = 6$	m) $b = 9$	n) $g = 1, g = 6$
p) $a = 0, a = -6$			o) $x = 4, x = -9$
17: a) $(4t - 3)(3t - 1)$	b) $(4s + 1)(9s + 1)$	c) $(d + 3)(4d - 1)$	d) $(5c - 2)(8c + 1)$
e) $(8v + 1)(3v - 2)$	f) $(5r - 1)(10r - 1)$	g) $(u - 9)(5u + 2)$	h) $(6q - 1)(2q - 5)$
18: a) $m = 2\frac{1}{4} \pm \frac{1}{4}\sqrt{113}$	b) $b = -\frac{7}{10} \pm \frac{1}{10}\sqrt{89}$	c) $e = \frac{5}{6} \pm \frac{1}{6}\sqrt{37}$	d) $n = \frac{1}{2} \pm \frac{1}{2}\sqrt{5}$
e) $t = 1 \pm \frac{2}{5}\sqrt{10}$	f) $f = \frac{7}{8} \pm \frac{1}{8}\sqrt{113}$	g) $w = 1 \pm \frac{1}{3}\sqrt{21}$	h) $a = -1\frac{2}{3} \pm \frac{1}{3}\sqrt{13}$
19: a) $x = -3$ and $v = 4$ $x = 4$ and $v = -17$	b) $r = 2$ and $k = 6$ $r = 3$ and $k = 8$	c) $j = -4$ and $c = 23$ $j = -2$ and $c = 13$	d) $q = -3$ and $z = -17$ $q = -2$ and $z = -13$
e) $n = -1$ and $h = -7$ $n = 2$ and $h = 8$	f) $y = -2$ and $b = -2$ $y = 3$ and $b = -7$	g) $w = 3$ and $s = 17$ $w = 4$ and $s = 21$	h) $l = -2$ and $t = 12$ $l = 5$ and $t = -23$
20: a) $\frac{3(f+1)}{2(f+2)}$	b) $\frac{2v-3}{3v-1}$	c) $\frac{5(3a+1)}{4}$	d) $\frac{2(d+4)}{3}$
g) $\frac{2(u-1)}{5}$	h) $\frac{q-3}{2q-1}$	i) $\frac{4(m-2)}{3(m-4)}$	j) $\frac{3c+2}{3c-2}$
			k) $\frac{k+2}{3(3k+1)}$
			l) $\frac{3x-1}{2}$

$$\text{m) } \frac{j-1}{j+3}$$

$$\text{n) } \frac{3(2r+3)}{5}$$

$$\text{o) } \frac{e+1}{5(e-4)}$$

$$\text{p) } \frac{2g-3}{2g+1}$$

$$21: \text{ a) } \frac{3s-9}{6} - \frac{2s-1}{6} = \frac{s-8}{6}$$

$$\text{b) } \frac{6n+4}{6} + \frac{3n+12}{6} = \frac{9n+16}{6}$$

$$\text{c) } \frac{z-2}{4} + \frac{2z-2}{4} = \frac{3z-4}{4}$$

$$\text{d) } \frac{21y-14}{8} - \frac{12y-4}{8} = \frac{9y-10}{8}$$

$$\text{e) } \frac{6d+9}{15} + \frac{30d+10}{15} = \frac{36d+19}{15}$$

$$\text{f) } \frac{7t+14}{10} - \frac{2t-6}{10} = \frac{5t+20}{10} = \frac{5(t+4)}{10} = \frac{t+4}{2}$$

$$\text{g) } \frac{4w-6}{18} + \frac{15w-30}{18} = \frac{19w-36}{18}$$

$$\text{h) } \frac{6v+6}{9} - \frac{4v-2}{9} = \frac{2v+8}{9} = \frac{2(v+4)}{9}$$

$$\text{i) } \frac{2b-8}{12} + \frac{3b+12}{12} = \frac{5b+4}{12}$$

$$\text{j) } \frac{3u+2}{8} + \frac{6u+18}{8} = \frac{9u+20}{8}$$

$$\text{k) } \frac{12m+6}{10} - \frac{5m-10}{10} = \frac{7m+16}{10}$$

$$\text{l) } \frac{9c-9}{10} - \frac{15c-5}{10} = \frac{-6c-4}{10} = \frac{-2(3c+2)}{10} = \frac{-(3c+2)}{5}$$

$$\text{m) } \frac{r+2}{6} + \frac{12r+4}{6} = \frac{13r+6}{6}$$

$$\text{n) } \frac{5a+5}{20} - \frac{6a-4}{20} = \frac{-a+9}{20} = \frac{-(a-9)}{20}$$

$$\text{o) } \frac{3h-12}{12} + \frac{16h+8}{12} = \frac{19h-4}{12}$$

$$\text{p) } \frac{12k+18}{9} - \frac{2k-6}{9} = \frac{10k+24}{9} = \frac{2(5k+12)}{9}$$

$$22: \text{ a) } \frac{12}{35f^2}$$

$$\text{b) } \frac{9g}{4} \times \frac{2g}{5} = \frac{18g^2}{20} = \frac{9g^2}{10}$$

$$\text{c) } \frac{3q}{2} \times \frac{4}{3q} = \frac{12q}{6q} = 2$$

$$\text{d) } \frac{63j}{4j} = \frac{63}{4}$$

$$\text{e) } \frac{7I}{6} \times \frac{10}{3I} = \frac{70I}{18I} = \frac{35}{9}$$

$$\text{f) } \frac{81p}{70p} = \frac{81}{70}$$

$$\text{g) } \frac{21}{35e^2} = \frac{3}{5e^2}$$

$$\text{h) } \frac{4}{5x} \times \frac{9}{5x} = \frac{36}{25x^2}$$

$$\text{i) } \frac{5}{8n} \times \frac{9n}{8} = \frac{45n}{64n} = \frac{45}{64}$$

$$\text{j) } \frac{24s}{35s} = \frac{24}{35}$$

$$\text{k) } \frac{8d}{3} \times \frac{5}{3d} = \frac{40d}{9d} = \frac{40}{9}$$

$$\text{l) } \frac{80u}{49u} = \frac{80}{49}$$

$$\text{m) } \frac{18}{28b^2} = \frac{9}{14b^2}$$

$$\text{n) } \frac{6v}{7} \times \frac{2}{5v} = \frac{12v}{35v} = \frac{12}{35}$$

$$\text{o) } \frac{9w}{10} \times \frac{9w}{5} = \frac{81w^2}{50}$$

$$\text{p) } \frac{18m}{24m} = \frac{3}{4}$$